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The 892 unique ways to partition a 3 x 4 grid

This poster illustrates a change in design practice. Computation-based design—that is, the use of algorithms to compute options—is becoming more practical and more common. Design tools are becoming more computationbased; designers are working more closely with programmers; and designers are taking up programming.

Above, you see the 892 unique ways to partition a 3 × 4 grid of the same configuration. The poster includes only unique into unit rectangles. For many years, designers have used grids to unify diverse sets of content in books, magazines, screens, and other environments. The 3 × 4 grid is a common example. Yet even in this simple case, generating all the options has-until now-been almost impossible.

Patch Kessler designed algorithms to generate all the possible variations, identify unique ones, and sort themnot only for 3 × 4 grids but also for any n × m grid. He instantiated the algorithms in a MATLAB program, which output PDFs, which Thomas Gaskin imported into Adobe Illustrator to design the poster.

Rules for generating variations

The rule system that generated the variations in the poster was suggested by Bill Drenttel and Jessica Helfand who noted its relationship to the tatami mat system used in Japanese buildings for 1300 years or more. In 2006, Drenttel and Helfand obtained U.S. Patent 7124360 on this grid system—"Method and system for computer screen lay- of the largest element, preceding from left to right and top out based on recombinant geometric modular structure".

The tatami system uses 1 × 2 rectangles. Within a 3 × 4 grid, 1 × 2 rectangles can be arranged in 5 ways. They appear at the end of section 6.

Unit rectangles (1×1, 1×2, 1×3, 1×4; 2×2, 2×3, 2×4; 3×3 , 3×4) can be arranged in a 3×4 grid in 3,164 ways. Many are almost the same-mirrored or rotated versions variations—one version from each mirror or rotation group. Colors indicate the type and number of related non-unique variations. The variations shown in black have 3 related versions; blue, green, and orange have 1 related version; and magenta variations are unique, because mirroring and rotating yields the original, thus no other versions. (See the table to the right for examples.)

Rules for sorting The poster groups variations according to the number of non-overlapping rectangles. The large figures indicate the beginning of each group. The sequence begins in the upper left and proceeds from left to right and top to bottom. Each group is further divided into sub-groups sharing the same set of elements. The sub-groups are arranged according to the size of their largest element from largest to smallest. Squares precede rectangles of the same area; horizontals precede verticals of the same dimensions. Within subgroups, variations are arranged according to the position to bottom. Variations themselves are oriented so that the largest rectangle is in the top left. Black dots separate groups by size. Gray dots separate groups by orientation.

Where to learn more 703 × Black Grids have been described in design literature for at least Asymmetric 50 years. French architect Le Corbusier describes grid systems in his 1946 book, Le Modulor. Swiss graphic designer Karl Gerstner describes a number of grid systems 180° rotation or "programmes" in his 1964 book, Designing Programmes. The classic work on grids for graphic designers is Josef 61 × Blue Muller-Brockman's 1981 book, Grid Systems.

Patch Kessler explores the mathematical underpinnings of grid generation in his paper "Arranging Rectangles". www.mechanicaldust.com/Documents/Partitions_05.pdf

Thomas Gaskin has created an interactive tool for viewing Rotational symmetry variations and generating HTML. www.3x4grid.com Changed by horizontal and vertical reflection.

Design: Thomas Gaskin Creative Direction: Hugh Dubberly Algorithms: Patrick Kessler Patent: William Drenttel + Jessica Helfand

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Changed by horizontal reflection, vertical reflection, and

Top-bottom symmetry Changed by horizontal reflection and 180° rotation.

26 × Green

26 × Magenta

180° rotation.

vertical reflection, or

All three symmetries combined

Unchanged by horizontal reflection.



RЯ

Horizontal



Original Reflection Reflection Rotation

Vertical

R H

180°